A NEW METHOD OF IMPULSE NOISE REDUCTION IN
GRAY AND COLOR IMAGES BY FUZZY FILTER

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Abstract: Image Reduction is one of the most important image processing tasks. In this article, a new fuzzy filter is presented for the removal of impulse noise in gray and color images. The filter consists of two stages. In the first stage, using trapezoid membership function four values are used to detect whether a given pixel contains noise or not. In the second stage fuzzy enhanced classifier is applied successively to remove the impulse noise in gray and color images. Experimental results are obtained to show the feasibility of the proposed approach. These results are also compared to other filters by numerical measures and visual inspection.

Keywords: Threshold, impulse noise, denoising, fuzzy filter, fuzzification, defuzzification

1. INTRODUCTION
Image processing has become a very important subject in electronic and computer engineering. Image processing has got wide varieties of applications in computer vision, multimedia communication, and television broadcasting etc., that demand very good quality of images.

1.1 NOISE
An image gets corrupted with noise during the process of acquisition, transmission, storage and retrieval. Noise may be classified as substitutive noise, impulsive noise (salt and pepper noise, random valued impulse noise etc.), and additive noise e.g. additive with Gaussian noise. Image restoration is one of the many areas it encompasses.

1.1.1 Impulse Noise
The probability density function of impulse noise is given by

\[ P(z) = \begin{cases} 
P_a & \text{for } z = a \\
0 & \text{otherwise} \\
 \end{cases} \]

If \( b > a \), gray level \( b \) will appear as a light dot in the image. Impulse noise is generally digitized as pure white or black values in an image. If they are equal to the minimum and maximum allowed values in the digitized image, they are called standard values. As a consequence, negative impulses appear as black (pepper) points in an image. Positive impulses appears as white (salt) noise. In an 8 bit image, \( a = 0 \) (black) and \( b = 255 \) (white). Fat fail distributed or impulse noise are sometimes called salt & pepper noise or spike noise. An image containing salt & pepper noise will have dark pixels in bright regions & bright pixels in dark regions. This type of noise can be caused by analog to digital converter errors, bit errors in transmission etc.

1.2 IMAGE DENOISING
It is one of the main areas of image restoration. Image denoising is usually required to be performed before display or further processing like segmentation feature extraction, object recognition, texture analysis etc. The purpose of denoising is to suppress the noise quite efficiently while retaining the edges and other detailed features as much as possible. It becomes necessary to suppress the noise quite effectively without distorting the edges and the fine details of the image so that the filtered image becomes more useful for display and/or further processing. The nature of denoising depends on the type of the noise corrupting the image. S. Schulte et.al [1] proposed a filter removing random impulse noise using fuzzy random method and Stefan Schulte et.al [2] presented a fuzzy filter to remove noises in color images. Morillas, S et al [3] presented fuzzy bilateral filtering for color images. In the literature [4]-[9] there are many methods available to remove impulse noise in gray scale and color images. Many filtering techniques over decades serve better for the enhancement of the images. Of these, Median Filter is the non-linear filter in which sorting operation is performed on the input vector. The job is done as the mid value is taken as the input. Moving average filter overcomes the drawback of the median filter by using moving average in which the value at the central pixel is replaced by the mean value of the corresponding input neighborhood. Entropy filter denoises image by replacing every value by the information entropy of the values in its range \( r \) neighborhood. The range filter allows to select a range of values. The left and right drag box can be used to change the lower and upper limit of the range, meaning that only rows with values within the chosen range remain in the visualization. An important feature of the range filter is that the values are distributed on a linear scale according to the values of the data. Standard filter filters image by replacing every value by the standard deviations of the values in its range \( r \) neighborhood. This paper deals with a new fuzzy filtering technique for the removal of impulse noise in both gray and color images. Fuzzy filters are easy to realize by means of simple fuzzy rules.

2. PROPOSED NEW FUZZY FILTER FOR
IMPULSE NOISE REDUCTION IN GRAY
AND COLOR IMAGES
This paper focuses on developing a new filter to remove impulse noise in gray and color images. The proposed filter uses fuzzy trapezoid membership function to remove impulse noise in the image. Let \( f(x, y) \) and \( f'(x, y) \) denote the pixel value at location \( (x, y) \)
of the given input image and the image with the noise respectively.

The impulse noise detection with noise α is given as follows

\[
f(x, y) = \begin{cases} 
\frac{E_{x,y}}{\alpha} & \text{with the probability } \alpha \\
Q_{x,y} & \text{with probability } 1 - \alpha 
\end{cases} \quad (2.1)
\]

where \(E_{x,y}\) denotes the noise value

\[\text{Deten} = \text{abs}(f_i - f_j) \quad (2.2)\]

By using fuzzy trapezoid membership classification, four values are used to detect whether a given pixel contains noise or not. The trapezoid membership classification is used because the deployment of the trapezoidal membership function is better than the triangular membership function. In addition, trapezoidal function provides the optimal degree of compatibility for higher levels of attributes than the triangular function. At the same time, it is provided with the maximum membership value which corresponds to the centroid of the triangular shape. As a result, the application of trapezoidal membership function using enhanced fuzzy classifier gives higher degrees of compatibility resulting in the approximation of the desired output. To use trapezoidal membership function, four parameters are necessary as given in figure 2.1, and so 4 x 4 matrix is used.

![Figure 2.1 Trapezoidal membership function](image)

By applying the trapezoidal membership function, initially, Deten, is mapped onto range [0,100] and are classified into two partitions. The two partitions comprise low Deten, (L) and high intensity Deten, (H) respectively using two different thresholds, namely \(T_1\) and \(T_2\).

If (Deten,isin range \((0,T_1)\)

(pixel is classified as Deten, (L)))

Else

If (Deten,isin range \((T_1,100)\)

(pixel is classified as Deten, (H)))

Endif

Let us consider a scenario, a process followed to restore the noisy images.

**Table 2.1 Impulse noise reduction process**

<table>
<thead>
<tr>
<th>240</th>
<th>120</th>
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<td>240</td>
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</tr>
</tbody>
</table>

a) pixel - original image  
b) Pixel – noisy image

The motivation for Impulse noise detection and filtering using Fuzzy Classification of noisy images is illustrated as follows. In Table 2.1(a), the original image of a pixel is shown. Let us consider that the two pixels in the image block comprise of impulse noise with the respective noisy pixel values as 250 and 180 as illustrated in Table 2.1(b). Then, in this case scenario, let us assume that the locations of these two impulse noisy pixels are detected and replaced using enhanced fuzzy classification as shown in Table 2.1(c).

When compared with Table 2.1(a) and Table 2.1(c), one noisy pixel is restored after application of first membership function. The impulse noisy pixel value 180 is replaced with the value of 160 which also comprise of impulse noise pixel value when compared to the actual original pixel value of the corresponding image. Subsequently, if we repeat the same process by applying the membership function, then both noisy pixels are removed as illustrated in Table 2.1(d).

The original cameraman image, the impulse noise image is shown in figure 2.2.

![Figure 2.2 Impulse Noise Reduction Process](image)

**Figure 2.2 Impulse Noise Reduction Process**

The quality of images using fuzzy classification is measured by means of peak signal-to-noise ratio (PSNR), detection accuracy and noise level.

3. Experimental Results Impulse noise detection and filtering using Enhanced Fuzzy Classifier

In order to assess the performance of the proposed Impulse Noise Removal using Enhanced Fuzzy Classifier(INREFC), extensive simulations are carried out on standard gray and color images of cameraman under different noisy conditions in MATLAB. The performance is measured in terms of Peak Signal-to-Noise Ratio (PSNR) detection accuracy and noise level.

PSNR is defined as

\[
\text{PSNR} = 10 \log_{10} \left( \frac{255^2}{\text{MSE}} \right) \text{dB}
\]
Detection accuracy is defined as

\[ \text{Detection Accuracy} = \frac{1}{N} \sum_{i=1}^{N} \sqrt{x_i^2 + y_i^2} \]

3.1 Measure of PSNR

The table below shows the peak signal-to-noise rate for different image sizes which is obtained using gray images of cameraman.

<table>
<thead>
<tr>
<th>Image Size (pixels)</th>
<th>PSNR (dB)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Proposed</td>
</tr>
<tr>
<td>150</td>
<td>93</td>
</tr>
<tr>
<td>200</td>
<td>93.55</td>
</tr>
<tr>
<td>250</td>
<td>95</td>
</tr>
<tr>
<td>300</td>
<td>96.5</td>
</tr>
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</table>

3.2 Measure of Detection Accuracy

The table given below shows the detection accuracy rate for different image sizes which is obtained using color and gray images of cameraman.

<table>
<thead>
<tr>
<th>Image Size (pixels)</th>
<th>Detection Accuracy (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Proposed INREFC</td>
</tr>
<tr>
<td>150</td>
<td>65</td>
</tr>
<tr>
<td>200</td>
<td>70</td>
</tr>
<tr>
<td>250</td>
<td>72</td>
</tr>
<tr>
<td>300</td>
<td>75</td>
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</table>
5-10% reduced when compared to range filter.

4. CONCLUSION

An enhanced approach has been proposed for the removal of impulse noise using enhanced fuzzy classifier. The main advantages of this filter are the denoising capability and suitability for both gray and color images. A numerical measure, such as PSNR, detection accuracy, noise level have shown convincing results. Moreover, we have shown that the proposed method achieves a more comparable noise reduction performance than the other existing filters. Our future work will be on focusing reduction of speckle noise, stripping noise etc., in gray and color images.

5. REFERENCES


